# Reconstructing cancer genomes <br> from paired-end sequencing data 

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## Genome of a cancer tumor

Comprised from the germline genome through a series of structural variations.


| 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- |



Schematic diagram of rearranged genome

## Greenman 2011

Changed chromosome 9

BCR-ABL fusion gene in chronic myeloid leukemia



Breast tumor HCC1954

## Paired-end read

- Sample DNA sequence $S$ is cut into small fragments (200-500 bp)
- Each end of the fragment ( 36 bp ) is then aligned against a reference genome $R$.
- Concordant reads - both ends aligned to the same distance
- Discordant reads - ends are aligned to a different distance.



## Genome reconstruction

From the reads we derive:

- A sequence of intervals $I=\left(I_{1}, I_{2}, \ldots, I_{n}\right)$. Each Interval $I_{j}=\left[s_{j}, t_{j}\right]$.
- From discordant reads: a set of adjacencies

$$
A \subseteq\left\{\left(I_{j}, I_{k}\right) \mid j, k \in\{ \pm 1, \pm 2, \ldots, \pm n\}\right\}
$$

- From concordant reads: a read depth vector $r=\left(r_{1}, \ldots, r_{n}\right)$, where $r_{j}$ is the number of reads that fall entirely within $I_{j}$.


# Copy number and adjacency genome reconstruction problem 

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2. Cancer genomes may be aneuploid.
3. A tumor is not genetically homogenous.

## Single Chromosome copy number and

 adjacency genome reconstruction problemGiven an interval vector $I$, a set $A$ of cancer adjacencies, an interval count vector $c$, and the set $R$ of reference adjacencies, find a cancer genome $I_{\alpha(1)} I_{\alpha(2)} \ldots I_{\alpha(M)}$ satisfying:

1. $\forall_{1 \leq j \leq M-1}\left(I_{\alpha(j)}, I_{\alpha(j+1)}\right) \in A$ or $\left(I_{\alpha(j)}, I_{\alpha(j+1)}\right) \in R$.
2. For $=1, . ., n$, the total number of indices $j$ with

$$
\alpha(j)=k \text { or } \alpha(j)=-k \text { is equal to } c_{k}
$$

## Interval-adjacency graph

- Undirected graph G(V,E)

$$
\begin{aligned}
& V=\left\{s_{1}, t_{1}, s_{2}, t_{2}, \ldots, s_{n}, t_{n}\right\} \\
& E=E_{I} \cup E_{R} \cup E_{V}
\end{aligned}
$$

- Interval edges

$$
\begin{aligned}
& E_{I}=\left\{e_{I}(j)=\left(s_{j}, t_{j}\right)\right\} \\
& E_{R}=\left\{\left(t_{j}, s_{j+1}\right)\right\} \\
& E_{V}=\left\{\left(t_{i} / s_{i}, s_{j} / t_{j}\right) \mid\right. \\
& \left.\qquad \quad\left[I_{i /-i}, I_{j /-j}\right] \in A\right\}
\end{aligned}
$$

- Reference Edges $E_{R}=\left\{\left(t_{j}, s_{j+1}\right)\right\}$
- Variant edges

Reference Genome:


A block organization of the cancer genome corresponds to a path along the graph that:

1. Starts at $s_{1}$ and ends at $t_{n}$
2. Alternates between interval edges and non-interval edges.
3. The number of times each interval edge is traversed is equal to $c_{j}$


## Perfect data

- Assume that $c$ is known and that $A$ is accurate.
- We need to find the copy number of the variant edges - $\mu$.
- This can be formulated as an ILP problem with the constraint:

$$
\mu\left(e_{I}(v)\right)=\mu\left(e_{R}(v)\right)+\sum_{a \in E_{A(v)}} \mu(a)
$$



- Given the edge weights $\mu$, finding an alternating path corresponds to the problem of finding an alternating Eulerian Tour in the multigraph $G_{\mu}=\left(V, E_{\mu}\right)$.
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Tour in the multigraph $G_{\mu}=\left(V, E_{\mu}\right)$.
- In the case of multiple chromosomes we simply require multiple edge disjoint alternating paths.
- When the data is perfect at least one such solution exists.


## Imperfect data

- $A$ is not accurate and $c$ is unknown.
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- $A$ is not accurate and $c$ is unknown.
- Instead we have a read depth vector r.
- Let $L_{1}, L_{2}, \ldots L_{n}$ be the lengths of $I_{1}, I_{2}, \ldots I_{n}$.
- Let $L_{R}=\sum_{i=1}^{n} L_{i}$, be the length of the reference genome.
- Let $N=\sum_{i=1}^{n} r_{i}$, be the total number of concordant reads aligned within an interval.


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$$

- In a rearranged genome:

$$
\lambda_{j}\left(\frac{\mu}{\tau}\right)=\frac{N L_{j}}{L_{R}} \times\left(\frac{\mu}{\tau}\right)
$$

- Where $\tau=2$ is the expected number of copies of each interval.
- To find the weights of the edges $\mu$, we define a (negative) likelihood function:

$$
L_{r}(\mu)=\sum_{j} \lambda_{j}\left(\frac{\mu_{j}}{\tau}\right)-r_{j} \log \left(\lambda_{j}\left(\frac{\mu_{j}}{\tau}\right)\right)
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- Thus we have the following formulation:

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- Subject to:

$$
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- Introduce intervals $>8 \mathrm{~Kb}$
- Analysis restricted to 22 autosomes


## Results - used variant edges

| Dataset | ID | \#Var Edges | Used | $\%$ |
| :---: | :---: | :---: | :---: | :---: |
| OV1 | TCGA-13-0890 | 771 | 499 | $65 \%$ |
| OV2 | TCGA-13-0723 | 562 | 268 | $48 \%$ |
| OV3 | TCGA-24-0980 | 311 | 172 | $55 \%$ |
| OV4 | TCGA-24-1103 | 340 | 218 | $64 \%$ |
| OV5 | TCGA-13-1411 | 389 | 255 | $66 \%$ |



Figure 2: Cancer Genome Reconstruction for OV2 when a minimum of 10 discordant pairs are required to add a variant edge to the graph.


Node Labels


Telomeric


Regular
Truncated


Edge Types
Interval Edge $\qquad$
Reference Edge $\qquad$
Variant Edge ———

Figure 5: Cancer Genome Reconstruction for OV5 when a minimum of 10 discordant pairs are required to add a

## Reciprocal vs non-reciprocal variants



Non-Reciprocal Inversion


Reciprocal Translocation


Non-Reciprocal Translocation


Non-Reciprocal Robertsonian Translocation

## Trivial reciprocal edges

reciprocal edges are "trivial" if the multiplicities of the two variant edges are equal and for each pair of interval edges of the corresponding breakpoints, their multiplicity is equal as well.

"Trivial"


Non trivial

## Fishers exact test for variant edges

| Dataset | variant Type | Reciprocal, Trivial, Used | Reciprocal, non Trivial, Used | Reciprocal, Trivial, non Used | Reciprocal, non Trivial, non Used | non Reciprocal, non Trivial, Used | non Reciprocal, non Trivial, non Used | p Val |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| OV1 | T | 104 | 75 | 28 | 13 | 9 | 58 | <1E-15 |
| OV1 | 1 | 30 | 16 | 8 | 12 | 2 | 29 | 3.46E-05 |
| OV1 | TO | 140 | 70 | 30 | 16 | 9 | 38 | $2.79 \mathrm{E}-12$ |
| OV2 | T | 36 | 41 | 28 | 23 | 12 | 49 | 5.17E-07 |
| OV2 | 1 | 12 | 9 | 10 | 5 | 10 | 21 | $5.70 \mathrm{E}-02$ |
| OV2 | TO | 50 | 46 | 46 | 18 | 15 | 44 | 2.63E-07 |
| OV3 | T | 42 | 19 | 10 | 3 | 6 | 30 | 2.11E-07 |
| OV3 | I | 14 | 5 | 8 | 5 | 2 | 13 | $7.50 \mathrm{E}-02$ |
| OV3 | TO | 36 | 22 | 18 | 8 | 7 | 28 | 1.92E-05 |
| OV4 | T | 34 | 40 | 10 | 6 | 12 | 35 | $1.54 \mathrm{E}-09$ |
| OV4 | 1 | 8 | 2 | 0 | 0 | 3 | 12 | 7.30E-02 |
| OV4 | TO | 26 | 22 | 12 | 10 | 12 | 26 | $3.60 \mathrm{E}-02$ |
| OV5 | T | 64 | 29 | 12 | 7 | 8 | 37 | $2.30 \mathrm{E}-08$ |
| OV5 | 1 | 10 | 2 | 8 | 0 | 6 | 13 | $1.30 \mathrm{E}-01$ |
| OV5 | TO | 60 | 22 | 18 | 8 | 7 | 34 | $2.29 \mathrm{E}-06$ |

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Conclusion: it may be easier to satisfy the copy number balance conditions for vertices associated with reciprocal variant.

## Simulated Data

- Simulate a cancer genome $C$.
- Simulate pair-end reads on $C$.
- Model a heterogeneous tumor by sampling $\rho$ percentage of the samples from a reference genome.
- Add Gaussian noise to each $r_{j}$ drawn from $N\left(0, \phi r_{j}\right)$


## Simulated Data - results



Figure 6 Simulations. Effect of sample contamination and read depth estimation errors on a simulated cancer genome. $\varphi$ is a scaling factor for the variance; for example $\varphi=400$ means that the noise model has a standard deviation 20 times $r_{j}$ for interval $I_{j}$. We show the average percent of interval edges (left) and reference and variant edges (middle) correctly estimated over 10 trials. (Right) At $\rho=0$, as $\varphi$ increases most of the errors result from variant edges moving from the correct multiplicity of 1 (heterozygous deletion) to a multiplicity of 2 (homozygous deletion).

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- Mapping discordant reads in repetitive areas can be difficult.
- Read depth estimation as well.
- Many paths may agree with the graph.
- Estimated edge multiplicities may not be unique.
- No allele-specific information.
- A cancer sample is heterogeneous.


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